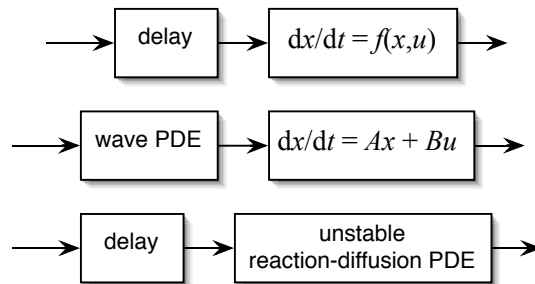


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Delay Compensation in Nonlinear, Adaptive, and PDE Systems



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